



## Definition 2: Epistemic Types

- Directly represent uncertainty over utility function using the notion of **epistemic type**.



### Definition

A **Bayesian game** is a tuple  $(N, A, \Theta, p, u)$  where

- $N$  is a set of agents,
- $A = (A_1, \dots, A_n)$ , where  $A_i$  is the set of actions available to player  $i$ ,
- $\Theta = (\Theta_1, \dots, \Theta_n)$ , where  $\Theta_i$  is the type space of player  $i$ ,
- $p : \Theta \mapsto [0, 1]$  is the common prior over types,
- $u = (u_1, \dots, u_n)$ , where  $u_i : A \times \Theta \mapsto \mathbb{R}$  is the utility function for player  $i$ .

# Definition 2: Example



	$I_{2,1}$	$I_{2,2}$																
$I_{1,1}$	<table border="1"><tr><td colspan="2">MP</td></tr><tr><td>2, 0</td><td>0, 2</td></tr><tr><td>0, 2</td><td>2, 0</td></tr><tr><td colspan="2"><math>p = 0.3</math></td></tr></table>	MP		2, 0	0, 2	0, 2	2, 0	$p = 0.3$		<table border="1"><tr><td colspan="2">PD</td></tr><tr><td>2, 2</td><td>0, 3</td></tr><tr><td>3, 0</td><td>1, 1</td></tr><tr><td colspan="2"><math>p = 0.1</math></td></tr></table>	PD		2, 2	0, 3	3, 0	1, 1	$p = 0.1$	
MP																		
2, 0	0, 2																	
0, 2	2, 0																	
$p = 0.3$																		
PD																		
2, 2	0, 3																	
3, 0	1, 1																	
$p = 0.1$																		
$I_{1,2}$	<table border="1"><tr><td colspan="2">Coord</td></tr><tr><td>2, 2</td><td>0, 0</td></tr><tr><td>0, 0</td><td>1, 1</td></tr><tr><td colspan="2"><math>p = 0.2</math></td></tr></table>	Coord		2, 2	0, 0	0, 0	1, 1	$p = 0.2$		<table border="1"><tr><td colspan="2">BoS</td></tr><tr><td>2, 1</td><td>0, 0</td></tr><tr><td>0, 0</td><td>1, 2</td></tr><tr><td colspan="2"><math>p = 0.4</math></td></tr></table>	BoS		2, 1	0, 0	0, 0	1, 2	$p = 0.4$	
Coord																		
2, 2	0, 0																	
0, 0	1, 1																	
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BoS																		
2, 1	0, 0																	
0, 0	1, 2																	
$p = 0.4$																		

$a_1$	$a_2$	$\theta_1$	$\theta_2$	$u_1$	$u_2$
U	L	$\theta_{1,1}$	$\theta_{2,1}$	2	0
U	L	$\theta_{1,1}$	$\theta_{2,2}$	2	2
U	L	$\theta_{1,2}$	$\theta_{2,1}$	2	2
U	L	$\theta_{1,2}$	$\theta_{2,2}$	2	1
U	R	$\theta_{1,1}$	$\theta_{2,1}$	0	2
U	R	$\theta_{1,1}$	$\theta_{2,2}$	0	3
U	R	$\theta_{1,2}$	$\theta_{2,1}$	0	0
U	R	$\theta_{1,2}$	$\theta_{2,2}$	0	0

$a_1$	$a_2$	$\theta_1$	$\theta_2$	$u_1$	$u_2$
D	L	$\theta_{1,1}$	$\theta_{2,1}$	0	2
D	L	$\theta_{1,1}$	$\theta_{2,2}$	3	0
D	L	$\theta_{1,2}$	$\theta_{2,1}$	0	0
D	L	$\theta_{1,2}$	$\theta_{2,2}$	0	0
D	R	$\theta_{1,1}$	$\theta_{2,1}$	2	0
D	R	$\theta_{1,1}$	$\theta_{2,2}$	1	1
D	R	$\theta_{1,2}$	$\theta_{2,1}$	1	1
D	R	$\theta_{1,2}$	$\theta_{2,2}$	1	2